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3 (Sem 4) PHY M1

2015 PHYSICS

(Major)

Theory Paper : M-4.1

Full Marks - 60

Time $-2\frac{1}{2}$ hours

The figures in the margin indicate full marks for the questions.

GROUP-A

1. Answer any *four* of the following questions : $1 \times 4 = 4$

(a) Define ordinary point of a second order differential equation.

(b) What is the value of $P_n(t)$?

- (c) Define total probability.
- (d) Under what condition does the Gaussian distribution become normal distribution ?

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- (e) Give an example where Legendre polynomial is used in Physics.
- (f) What is meant by mean deviation ?
- Answer any three of the following questions : $2\times 3 = 3$
 - (a) Check whether Frobenius method can **b** applied to the following equation or not.

$$\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} - \frac{9y}{x^3} = 0$$

(b) Prove that $P_n^m(-x) = (-1)^{n+m} P_n^m(x)$.

- (c) What is the probability that the ace of spaces will be drawn from a deck of cards at leas once in 104 consecutive trials ?
- (d) Prove the following recurrence relation $^{r_{t}} 2xH_{n}(x) = 2nH_{n-1}(x) + H_{n+1}(x);$
- (e) Find the degree and order of the following equation :

$$\left(\frac{\mathrm{d}^2 y}{\mathrm{d}x^2}\right)^{\frac{2}{3}} = \left(y + \frac{\mathrm{d}y}{\mathrm{d}x}\right)^{\frac{1}{2}}$$

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- 3. Answer any *two* of the following questions : $5 \times 2 = 10$
 - (a) Establish the following recurrence formula for Legendre polynomial $P_n(x)$

 $nP_n(x) = (2n-1)xP_{n-1}(x) - (n-1)P_{n-2}(x).$ 5

- (b) Find the singularity of the differential equation $(1-x^2)y'' + xy' + y = 0$ and discuss the nature of the singularity. 5
- (c) Find the probability of almost 5 defective fuses to be found in a box of 200 fuses, if experience shows that 2% of such fuses are defective.

(d) Show that
$$\int_{-1}^{+1} x P_n(x) P_{n-1}(x) dx = \frac{2n}{4n^2 - 1} \cdot 5$$

4. Answer any two of the following : $10 \times 2=20$

• ...

(a) (i) Using the following definition of the Legendre polynomials $P_n(x)$,

$$(1-2xt+t^2)^{-\frac{1}{2}} = \sum_{n=0}^{\infty} t^n P_n(x)$$

show that $|P_n \cos(\theta)| \le |$

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- (ii) Prove the recurrence relation $xP'_{n} P'_{n-1} = nP'_{n}$ 4
- (b) (i) Find the indicial equation of the Hermite

equation
$$\frac{d^2y}{dx^2} - 2x\frac{dy}{dx} + 2xy = 0.$$

 (ii) Show that the generating function for Hermite polynomial H_n(x), for integral n, and real values of n is given by

$$e^{2xt-t^2} = \sum_{n=0}^{\infty} \frac{t^n}{n!} H_n(x).$$

(c) (i) What is Gaussian distribution ?

(ii) Define standard deviation.

- (iii) Prove the theory of compound probability. 5
 - (iv) Write one property of normal distribution.

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(d) (i) Show that $\int_{-1}^{+1} P_n(x) P_m(x) dx = 0$

where $P_n(x)$ and $P_m(x)$ are solutions of the Legendre differential equation. 6

(ii) Show that

 $H_0(x) = 1$ and $H_1(x) = 2x$. 2+2=4

GROUP – B

5. Answer any two of the following : 1×2=2
(a) What is the function of control unit ?
(b) Give the logical AND operation.

(c) What is a string?

6. Answer any two of the following : $2 \times 2 = 4$

(a) Define with example an operating system.

(b) What are control statements ? Give examples.

(c) Write a syntax in C/FORTRAN. How is an array declared in a program ?

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7. Answer any one of the following :

(a) Write a program in FORTRAN/C/C⁺⁺ to find the sum of first n natural numbers.

(b) Draw a flow chart to find the factorial of a number.

8. Answer any one of the following questions :

^{10×1=10}

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- (a) Describe with a block diagram for the different functional units of a digital computer.
- (b) Write the algorithm and draw the flow chart to find the largest of N numbers. 5+5=10

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