3 (Sem-6) MAT M 2

2016

MATHEMATICS

(Major)

Paper : 6.2

(Numerical Analysis)

Full Marks : 60 Time : 3 hours

The figures in the margin indicate full marks for the questions

1. Answer the following questions : 1×7=7

- (a) What is meant by normalized floating point representation of real numbers?
- (b) Subtract 203.176 from 791.23 in normalized floating point representation.
- (c) Define relative error.
- (d) Define shift operator E.
- (e) Establish the relation $E = 1 + \Delta$.
- (f) Evaluate $\Delta^2 (3e^x)$.
- (g) What is meant by extrapolation?

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- **2.** Answer the following questions : 2×4=8
 - (a) What assumptions are to be kept in mind for interpolation?
 - (b) Show that $(1 + \Delta)(1 \nabla) = 1$, where the symbols have their usual meanings.
 - (c) Using normalized floating point representation, add 4546 E5 and .5433 E7.
 - (d) Find f(6); it is given f(0) = -3, f(1) = 6, f(2) = 8, f(3) = 12, the third difference being constant.
- **3.** Answer the following questions : 5×3=15
 - (a) Derive Newton's forward interpolation formula.
 - (b) Use the method of separation of symbols to prove the following identity :

$$u_{x} = u_{x-1} + \Delta u_{x-2} + \Delta^{2} u_{x-3} + \cdots + \Delta^{n-1} u_{x-n} + \Delta^{n} u_{x-n}$$

Or

Given

 $\sin 45^\circ = 0.7071$, $\sin 50^\circ = 0.7660$

 $\sin 55^\circ = 0.8192$, $\sin 60^\circ = 0.8660$

Find sin 52° by using any method of interpolation. Mention why you have chosen the particular method.

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- (3)
- (c) Find the real root of the equation $x^2 5x + 2 = 0$ correct to four places of decimal by using Newton-Raphson method.
- 4. Answer either (a) or (b) :
 - (a) (i) Derive Simpson's one-third rule.
 - (ii) Calculate an approximate value of

$$\int_0^{\pi/2} \sin x \, dx$$

by Simpson's rule using 11 ordinates.

- (b) (i) Derive Euler-Maclaurin summation formula.
 - (ii) Find the sum of

$$\frac{1}{51^2} + \frac{1}{53^2} + \frac{1}{55^2} + \dots + \frac{1}{99^2}$$

- 5. Answer either (a) or (b) :
 - (a) Explain briefly the idea of numerical integration. Establish the general quadrature formula and deduce trapezoidal rule from it. 2+5+3=10
 - (b) Derive Stirling's formula. Use Stirling's formula to find y₂₈, given

$$y_{20} = 49225, \ y_{25} = 48316, \ y_{30} = 47236,$$

 $y_{35} = 45926, \ y_{40} = 44306$

5+5=10

5

5

5

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(4)

6. Answer either (a) or (b) :

- (a) (i) Give the geometrical interpretation of Newton-Raphson method.
 - (ii) Prove that the bisection method always converges.

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(iii) Discuss the secant method with appropriate diagram.

- (b) (i) Find a real root of the equation $x^3 2x 5 = 0$ by the method of false position, correct to three decimal places.
 - (ii) Find the first, second and third derivatives of the function tabulated below at the point x = 1.5:

x	1.5	2.0	2.5	3.0	3.5	4.0
f(x)	3.375	7.000	13.625	24.000	38.875	59.000

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